

Cooking, Looking & Tweezing

Soft Matter Lab

March 18, 2025

Department of Physics & Chemistry of Soft Matter

# 1 Course Details

This course is divided into 5 parts (see Experiments) over 5 days. The final 2 days of this course are used to write the report (and catch up if required). You will perform the experiments and write the report.

## 1.1 General Information

This course is open to Science, Chemistry, Molecular Life Science and Physics students. The 3rd year Soft Matter Lecture course is a recommended prerequisite. The study load for this practical course is 3 EC (84 hours). This is built up as follows:

- 60 hours laboratory work
- 24 hours individual study (reading and preparation)

A lab-day will start at 08:30 and end at 17:00. Coffee breaks are from 10:10 to 10:30 and 15:10 to 15:30, lunch break is from 12:45 to 13:30. In case you cannot attend as a result of illness you should report yourself as sick by sending an email to [ruth.crothers@ru.nl](mailto:ruth.crothers@ru.nl) before the start of the practical.

The lab is typically completed in pairs, but in some cases you may be required to work alone. Each pair of students is expected to hand in one report on all experimental parts, including your Matlab code. Reports can be written in your preferred word processor, however we expect you to adhere to the layout detailed in Section 9. Your final grade will be calculated based on your answers in this handbook (25%), the final report (50%) and your in lab work (25%). In order to pass this course all of the above parts should be graded *pass*  $\geq 5.5$ .

## 1.2 Supervision and Organisation

This practical is organised and delivered by the Physics and Chemistry of Soft Matter Department.

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## 2 Introduction

The existence of atoms was first experimentally confirmed through the study of colloidal particles. By analysing the Brownian motion of these particles, scientists were able to determine Boltzmann's constant and subsequently Avogadro's number, thereby validating Einstein's theory on Brownian motion.

In this experiment, we will follow similar steps taken by Jean Perrin in the early part of the 20th century, to determine Avogadro's number. We will first synthesise colloidal particles, then build and use a brightfield microscope to image them. We use particle tracking routines in Matlab to determine the mean square displacement. Finally you will take part in optically trapping one of your colloids in one of our labs.

### 2.1 Outline

1. Synthesis of colloidal particles
2. Building a Brightfield Microscope
3. Imaging Colloids
4. Tracking Colloids using Matlab
5. Determination of Avogadro's number
6. Optical Trapping and Determination of Avogadro's number



- We will now derive the relationship between the Translational Diffusion Coefficient,  $D_T$ , and the Mean Squared Displacement (MSD).

1. First, rewrite the Langevin Equation in terms of displacement.

2. Multiply both sides of your equation by  $x$  and then rewrite as:

$$\frac{m}{2} \frac{d^2 x^2}{dt^2} = -m \left( \frac{dx}{dt} \right)^2 = Fx - \frac{\xi}{2} \frac{dx^2}{dt} + x f(t) \quad (1)$$

**HINT**  $\frac{d^2 x^2}{dt^2} = \frac{d}{dt} \left( \frac{dx^2}{dt} \right) = 2 \left[ x \frac{d^2 x}{dt^2} + \left( \frac{dx}{dt} \right)^2 \right]$

3. Next, by i) assuming that there is no external force, ii) taking the ensemble average and iii) then applying the equipartition theorem  $m\langle(\frac{dx}{dt})^2\rangle = k_B T$ , show that:

$$\frac{m}{2}\left\langle\frac{d^2x^2}{dt^2}\right\rangle - k_B T = -\frac{\xi}{2}\left\langle\frac{dx^2}{dt}\right\rangle \quad (2)$$

4. By taking  $z = \langle\frac{dx^2}{dt}\rangle$  integrate the above equation to obtain:

$$z = \frac{2k_B T}{\xi} + A \exp\left(-\frac{\xi t}{m}\right) \quad (3)$$

where  $A$  is a constant which does not depend on  $t$ .

5. Show that for long times  $t \gg \frac{m}{\xi}$  show that

$$\langle x^2 \rangle = \frac{2k_B T}{\xi} t = 2D_T t \quad (4)$$

6. Hence describe how  $D_T$  can be extracted from a particle trajectory.

Using the same resource, write a paragraph summarising both methods used by Perin to find Avagadro's number. It is best to work on these tasks in tandem with the synthesis.



## 4 Synthesising Colloids

In this section you will synthesise colloids from the organosilica compound 3-(trimethoxysilyl)propyl methacrylate (TPM). You are expected to complete the preparation work for the rest of the course in between the synthesis steps.

### 4.1 Learning Outcomes

- Understand the mechanism of synthesis of TPM colloidal particles

### 4.2 Materials

1. 10mM hydrochloric acid (HCl)
2. Azobisisobutyronitrile (AIBN)
3. 0.028 % ammonium hydroxide (NH<sub>4</sub>OH) (1×base)
4. Ultrapure water (MilliQ)

### 4.3 Procedure

1. Add 4.75 ml MilliQ + 0.25 ml 10 mM HCl + 0.5 ml TPM to a glass vial.
2. Stir vigorously for 1 hour. The resulting solution is referred to as hTPM.
3. In separate eppendorfs, set up the following;

	1	2	3	4	5	6	7	8	9	10	11
1×base ( $\mu$ l)	1000	900	800	700	600	500	400	300	200	100	50
hTPM ( $\mu$ l)	500	500	500	500	500	500	500	500	500	500	500

*Note:* Add hTPM to the eppendorf first then add the base quickly as one addition.

4. Leave to stand 1 hour.
5. Add a microspatula full of AIBN and place in oven for 3 hours, tumble every 30 minutes.
6. Leave to cool 30 minutes.
7. Wash and re-suspend with fresh MilliQ by centrifuging at 500 rcf for 10 minutes twice.

## 4.4 Hazards and Precautions

## 4.5 Discussion

1. Write the structure of TPM, identify hydrophobic and hydrophilic groups.
2. Write down the mechanism for steps 1) and 3) in the procedure.
3. What is the mechanism for droplet formation?
4. What is the main difference in the products from 1 to 11? How could you justify this difference?
5. What is the role of AIBN?

## 5 Building a Brightfield Microscope

In this section you will build a brightfield microscope to capture high magnification images of your colloids.

### 5.1 Learning Outcomes

- Understand the basic principles of ray tracing.
- Learn how to measure the focal length of a lens.
- Understand image formation in simple optical systems.

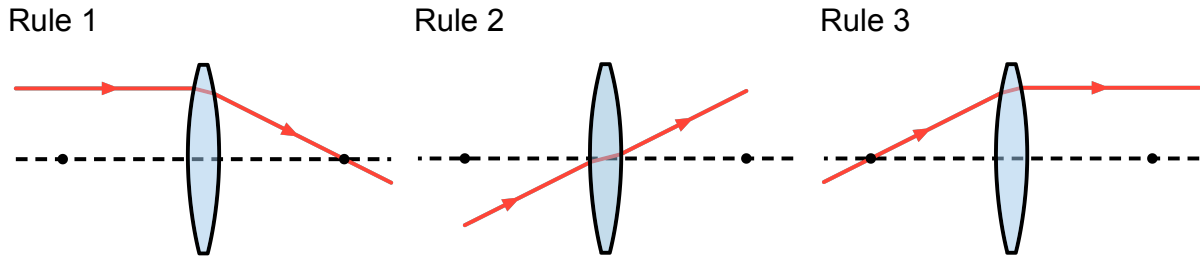
### 5.2 Equipment

- Camera
- Tube lens
- Microscope objective
- A ruler
- Alignment grid
- Various optomechanical components
- Illumination module

### 5.3 Basic Principles of a Simple Lens

Most optical systems can be reasonably described with the concept of refraction, and standardised definitions.

- Light rays entering a lens experience a transition from a low refractive index to a high refractive index (lens material). According to Snell's Law, the ray will bend towards the normal to the lens surface at the point of incidence.
- An optical axis is an imaginary line that passes through the centre of the lens and is perpendicular to the lens surfaces.
- All incident rays that are parallel to the optical axis are refracted by the lens to a converging point on the optical axis which is called the focal point.
- The distance from the lens to this focal point is called the focal length, and a plane normal to the optical axis at the focal point is called the focal plane.
- Optical diagrams are drawn from the left to the right. The object is traditionally placed on the left side of the optical system and the image is on the right side.



**Figure 1:** The basic rules of ray tracing for a simple lens.

### 5.3.1 Ray Tracing

Understanding how light propagates through optical elements can be well approximated by simplifying the light into lines called rays. This method is called ray tracing and is a fundamental concept in optics, where light-matter interactions are described by Snell's Law and rays are drawn along the optical system to give a good approximation of the optical behaviour of a given system. The three rules of ray tracing for a simple lens are shown in Figure 1 and described below;

1. Rays parallel to the optical axis (the central line perpendicular to the lens surfaces) will focus at the focal point on the right side of the lens. Rule 1 in Figure 1.
2. Rays that pass through the center of the lens will continue in a straight line without deviation. Rule 2 in Figure 1.
3. Rays that pass through the focal point on the left side of the lens will emerge parallel to the optical axis. Rule 3 in Figure 1.

### 5.3.2 Thin Lens Equation

The thin lens equation is a key principle in geometrical optics that describes the relationship between the focal length of a lens, the distance from the object to the lens, and the distance from the resulting image to the lens. It is used to predict how a lens will focus light from an object to form an image. You will use this to measure the focal length of your tube lens. The thin lens equation is given by,

$$\frac{1}{f} = \frac{1}{d_o} + \frac{1}{d_i},$$

where  $f$  is the focal length of the lens,  $d_o$  is the object distance and  $d_i$  is the image distance.

This equation assumes the lens is thin, meaning its thickness is negligible compared to the object and image distances.

## 5.4 Finding the focal length of a lens

Apply the ray tracing rules to Figure 2 and find the position and height of the image. By measuring the height of the formed image, the object distance,  $d_o$  and the image distance,  $d_i$  confirm that the magnification,  $M \approx \frac{d_i}{d_o}$ . Calculate the focal length of the lens in millimetres.

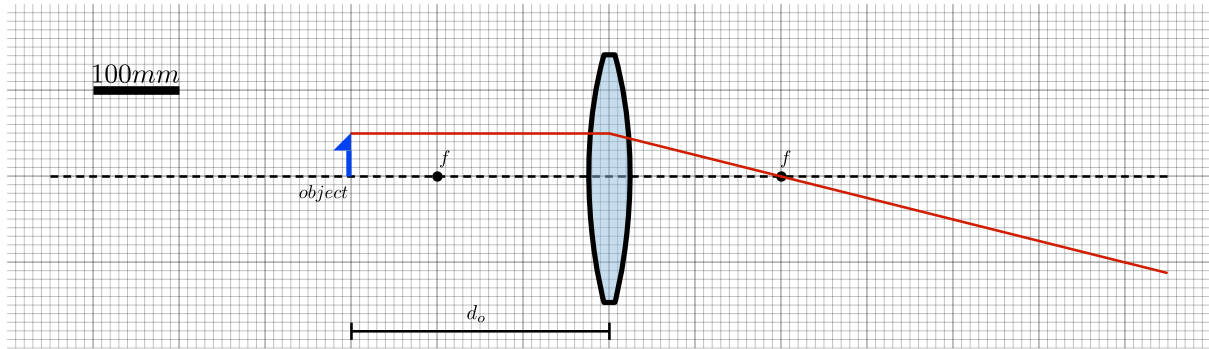


Figure 2: Forming an image with a single lens.

$$M =$$

$$f =$$

## 5.5 Find the focal length of your tube lens

First we will find a rough approximation of the focal length of the tube lens. This is done by forming an image of an approximated infinite light source (a ceiling light for example) on the surface of the floor. Measure the distance between the lens and the image to find the approximated focal length,  $f_{\approx}$ .

$$f_{\approx} =$$

Why is this method an approximate measure of the focal length? Is the measured focal length longer or shorter than the true focal length?

### 5.5.1 Image Formation with a Single Lens

Install the alignment target onto the end of four of the rods and install your tube lens at a distance of  $2f_{\approx}$  from the target. With the naked eye, find the position where the image of the grid is in focus. What do you notice about the image magnification?

Move your tube lens 25% closer to the alignment target (ie a distance of  $0.75 \times 2f_{\approx}$ ). Observe the image again with the naked eye. What do you notice about the image quality?

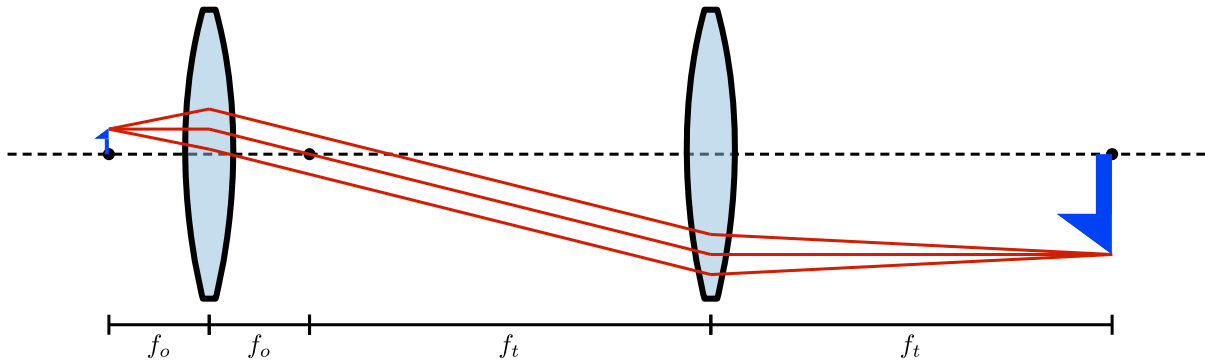


Figure 3: Image formation with an objective and tube lens.

## 5.6 Image Formation with Two Lenses

To form an aberration free, magnified image we need to place the object in the focal plane of the lens, however this would result in an image being formed at infinity from the lens (see thin lens equation). So we use two lenses. The first lens, the objective, collects light from the object and the tube lens forms an image at the focal plane of itself. To do this we need a more accurate measurement of the focal length of the tube lens.

### 5.6.1 Form an Image on the Camera

Place the alignment grid, tube lens and camera on the alignment rail. Using your approximated focal length of the tube lens, place the lens a distance of  $2f_{\approx}$  from the camera sensor. Now place the target grid on the opposite side of the lens and adjust its position until you see a clear image on the camera. Measure the distance between the lens and the target to find the true focal length of the tube lens,  $f_t$ . Position the tube lens exactly  $f_t$  from the camera sensor.

$f_t =$

## 5.7 Complete scope build

The set up you are building contains an objective and a tube lens which have different focal lengths. Consider the path of light through both lenses in the diagram below. What is the significance of using two lenses of different focal lengths?

Place the objective roughly a focal length in front of tube lens. Using your ruller position the objective such that the indicator mark on the objective is at a distance of  $f_{obj.} + f_t$  from the tube lens. Place the adaptor over the objective and switch on the illumination. Adjust the height of the microscope relative to the illumination until an image of the alignment grid is seen on the camera.

### 5.7.1 Calibrate the camera

Capture an image of the alignment target and measure the size in pixels (px) of the  $10\mu m$  grid. This gives you the pixels per micrometre calibration so you can convert your images to real world units.

Pixel Size =

### 5.7.2 Measure your microscopes magnification

Knowing the calibration above and the physical size of each camera pixel ( $2 \mu m$ ), calculate the magnification of your microscope.

Magnification =

Why is your magnification not that stated on your objective?

What is the focal length of your objective?





### 6.3 Imaging Parameters

A key in many-particle tracking is linking up particles positions in a time series of images to form a trajectory for each particle. In order to keep track of each particle, the displacement from image to image needs to be significantly smaller than the mean particle diameter. So we have to capture images at a frame rate that meets this requirement.

To estimate our frame rate we need to know the translational diffusion constant of our particles. This can be calculated from the Stokes-Einstein equation, defined in the Prep Work

Given that  $\langle x^2 \rangle = 2nD_T\tau$ , where  $n$  is the dimensionality, calculate the time,  $\tau$  it takes for a particle to move a distance equal to its diameter,  $d$ .

	1	2	3	4	5	6	7	8	9	10	11
$\tau(s)$											

What is the lowest frame rate you can use such that the colloid will be trackable from frame to frame?

Select one batch to continue with. What was the reasoning behind this choice?

Create a sample using the instructions in the sample preparation area. Ensure your colloids are diluted such that you end up with a monolayer of colloids when imaging them. Start with a dilution of 1  $mL$  of water to 1  $\mu L$  of colloid solution. Let your sample sediment for  $\approx 5$  minutes on the microscope then check to see if you have a monolayer.

Once you have a monolayer, check with a supervisor before capturing data. Using the frame rate you estimated earlier capture around 10 minutes of data.

## 7 Tracking and Analysis

In this section you will use Matlab to analyse your microscopy images.

The code can be downloaded from:

[github.com/Dullens-Lab/Matlab-Particle-Tracking/tree/SoftMatterPractical](https://github.com/Dullens-Lab/Matlab-Particle-Tracking/tree/SoftMatterPractical).

Ensure you download the SoftMatterPractical version .

Particle tracking can be divided into 3 main sections;

- Image Processing
- Particle Location
- Particle Tracking

In words, first the raw images are cleaned up, then the particle coordinates in each frame are found and finally these coordinates are linked up to form trajectories connected to an individual particle.

First you will work through a tutorial on image processing and particle location and then you will build these routines into a loop to find particles your own data. Finally the particle coordinates will be tracked.

- In Matlab open the file `Tutorial.m`.
- Use run section to load the example image into the workspace.
- Use the command `imagesc()` or `imshow()` to display the image.

### 7.1 Image Processing

Particle location relies on having good images where the only features are the colloids themselves. The image filtering step filters high and low frequency noise and applies a fixed background subtraction, such that the background equals a pixel value of 0. Open the function file `bpass.m` and read through the code.

- Define the arguments to the function.
- Run the function with one of your images and the following arguments, `bpass(image, true, true, 1, true)`.
- Change the value for the background until all the background is removed.
- Change the input for `hpass` and `lpass` to integers and explore the parameter space.
- Describe in words what high pass and low pass filtering do to an image.

## 7.2 Particle Location

Once the image is processed the particle locations can be found. This is a two step process, where the brightest pixels are found with `pkfnd.m` then these pixel coordinates are used by `cntrd.m` to calculate the subpixel coordinates of the particles.

- Open the function `pkfnd.m`.
- Define the inputs.
  
- Define the outputs.
  
- Run this section with the following inputs: `pkfnd(filtered, 10, 3)`
  
- Find the peaks in the raw and the filtered image, how would tracking unprocessed images affect results?

Once the peak pixels are found, the positions are refined by `cntrd.m`.

- Open the function `cntrd.m`.
- Write down the equation for finding the centre of the particle to a subpixel accuracy.
  
- Run the function with the following arguments,  
`cntrd(filtered, est_pks, 5, true, 1)`

Create a figure showing the starting image alongside the intermediate images, `img_hpass`, `img_lpass` and `img_out`. Create a second figure with two copies of `img_out` with the coordinates `est_pks` and `cntrds` overlain and highlight a good example of a particle that has been accurately located.

## 7.3 Create Tracking Loop

A convenient way to store information in Matlab is to use structures, where each field within a structure contains an array e.g. if `COORD` is a structure with one field, `cntrds`, the positions for frame `t` can be stored in `COORD(t).cntrds`.

Create a Matlab script that loops over all your images and stores each frames coordinates in structure called, for example, `COORD`. Ensure you suppress any image displays or

plotting during the loop iterations.

## 7.4 Particle Tracking

Once we have all the particle coordinates for all frames we need to link them up to form trajectories for each particle.

- Open the tracking function file, `trck.m`.
- Define the inputs.
- Define the outputs.
- Track the particles using their diameter as the maximum displacement.

## 7.5 Analyse Your Own Data

Run you tracking loop over your own data. (Note you will have to optimise the parameters for each step, you can use the tutorial script for this).

## 7.6 Mean Squared Displacement

What shape do you expect the MSD to be? What function should fit the line?

### 7.6.1 Calculate the MSD

- Import the MSD function into the correct workspace
- Run this function `input = (x y z t ID)`
- Output of this function is the ensemble averaged MSD, describe in a sentence how this averaging is being carried out.
- Plot the MSD versus time (in seconds)

### 7.6.2 Fitting the MSD

- Using the Matlab function `fit`, fit the MSD versus  $t(s)$  with the correct function.
- From this value determine  $D_T$ . What are the units?

- What is the value of  $D_T$  after fitting over 10 points vs 1000 points? Which is likely to be more accurate.

### 7.6.3 Calculate Avagadro's Number

Starting with Stokes-Einstein equation, use the Ideal Gas Laws to write down the relationship between Avagadro's number,  $N_A$  and  $D_T$ . From your measured  $D_T$  calculate Avagadro's Number.

## 8 Optical Trapping

In this section, you will use optical trapping to determine Avogadro's number. Optical trapping employs a laser to 'trap' a particle, enabling direct manipulation and measurement of individual colloids within a sample. Optical trapping forces rely on a refractive index mismatch between the colloid and the surrounding solvent.

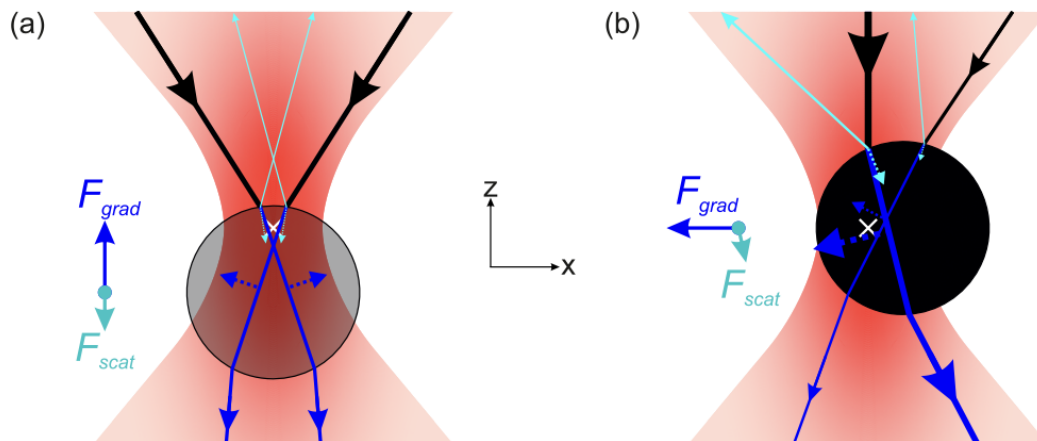
What type of light source is a laser?

Consider the Fig. 4 which shows a colloidal particle trapped within a laser beam and a particle displaced from the centre of the beam. Consider the first scenario:

- What two things happens to the incident ray when it hits the particle?
- Label the two resultant forces on the particle from both effects?
- Therefore explain why a refractive index mismatch between particle and solvent is important.

Consider the second scenario:

- What two things happens to the incident ray when it hits the particle?
- Label the two resultant forces on the particle from both effects?
- For the particle to be restored to the trap which force must be greater?



**Figure 4:** Forces in Optical Trapping.

Sample should be prepped in an identical way to the previous microscopy experiments.

## 8.1 Safety

In this section you will carry out this experiment in the laser lab of PCSM. This set up includes a Class IV laser, this is the most dangerous type of laser which can cause serious eye damage. You must adhere to the following safety procedures:

- Before entering the lab, laser safety glasses must be put on and verified by the supervisor.
- Whilst in the lab, Laser Safety glasses must not be removed for any reason.
- During your time in our laser lab you must avoid physical contact with the experimental system and the table upon which the system is installed.

**FAILURE TO FOLLOW THE INSTRUCTIONS WILL RESULT IN EXCLUSION FROM THE LAB.**

## 8.2 Analysis

- Using the particle location and tracking loop you developed previously calculate the MSD for the trapped particle.
- How is it different to the 'free' particle?

A particle on in a trap can be compared to a particle on a spring. We can determine the stiffness of the trap using Hooke's Law.

- What is Hooke's law for the potential energy of a spring?



$U(r)$  can be approximated as the  $-\ln(P(r))$ , where  $r$  is the displacement of the particle.

- Copy the code for MSD into a new file and adapt it to plot  $-\ln(P(r))$ .
- Fit this with the relation given by Hooke's Law to determine the trap stiffness.

The trap stiffness can be related to Boltzmann constant by the equation;

$$\langle x^2 \rangle = \frac{k_B T}{\kappa},$$

where  $\kappa$  is the trap stiffness.

- Use this relation to determine Boltzmann constant and in turn Avagadro's number.

- Which method was more accurate and why?

## 9 Report

You may use your preferred word processor to complete your report, but It should follow the following layout:

### 9.1 Introduction

Describe the work of Perrin (Prep work) and state the aim of this Practical.

### 9.2 Experimental Details and Theory

#### 9.2.1 Colloidal Model System

- Define a Colloid.
- Describe why colloids can be used as 'big atoms'.
- Define Brownian Motion, MSD and how to calculate  $D_T$ .

#### 9.2.2 Synthesis

- Explain mechanism of synthesis of colloidal particles from TPM.
- Outline Procedure followed.
- Include images and sizes for all batches.
- Include what batch was chosen for further experiments and why.

#### 9.2.3 Microscopy

- Include the diagram provided and draw the path of light through the set up.
- Define each component.
- Define the focal length and give the determined value.
- Give the determined pixel size of the camera and magnification of the microscope.
- Give the final image parameters and explain the values.

#### 9.2.4 Tracking

- Include the raw tutorial image as well as the same image after each step.
- Describe the process of image processing, particle location and tracking.

#### 9.2.5 Optical Trapping

- Include the diagram provided with the completed ray diagram.
- Describe the forces acting on the particle.
- Describe how the magnitude of the forces dictate if the particle remains in the trap.

## 9.3 Results

### 9.3.1 Determination of Avagadro's Number from MSD

- Show graph of MSD against time.
- Give value of  $D_T$  and NA.
- Explain any sources of discrepancy in your answer.
- How is this method an improvement on Perrin's work.

### 9.3.2 Determination of Avagadro's Number from $k_B$

- Show graph of MSD against time.
- Show graph of  $U$  vs  $r$ .
- Give value of  $k_B$  and NA.
- Explain any sources of discrepancy between your two values.

## 9.4 Conclusion

- How could this procedure be improved?
- Compare the value of NA from both methods, which was more accurate and why?